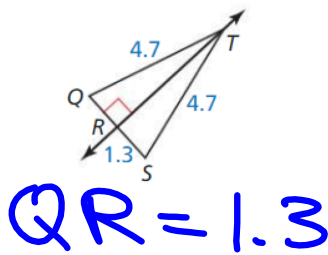


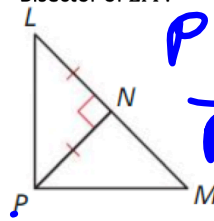
Bell Ringer

Monday 2/3

1. Find QR

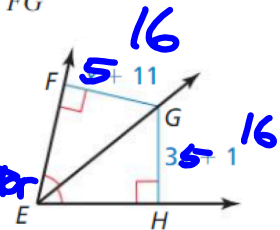


2. Which point is the perpendicular Bisector of \overline{LM} ?



P or N
 $\overline{PN} \perp \text{Bisector}$

3. Find FG



$$3x + 1 = x + 11$$

$$-x \quad -1 \quad -x \quad -1$$

$$2x = 10$$

$$x = 5$$

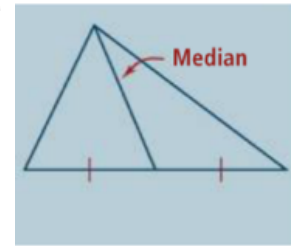
$FG = 16$

- Using your ruler draw a triangle,
- label each vertex A, B, and C on the inside.
- Cut out the triangle.

Find the midpoints of each side by:

- Fold vertex A until it touches vertex B and crease the side in the center of segment AB. Mark your crease with a point.
- Fold vertex A until it touches vertex C and crease the side in the center of segment AC. Mark your crease with a point.
- Fold vertex B until it touches vertex C and crease the side in the center of segment BC. Mark your crease with a point.
- Using a ruler, draw three lines that connect each vertex with the midpoint on the opposite side.

The segments drawn were **medians of the triangle**. The Median of a triangle is a segment whose endpoints are a vertex and the midpoint of the opposite side. The triangles three medians are always concurrent.



In a triangle, the point of concurrency of the medians is the **centroid of the triangle**. This is also the *center of gravity* of a triangle because it is where the triangular shape will balance. For any triangle, the centroid is always inside the triangle.

Label the point of concurrency D

Measure Each of your medians (from vertex A to the midpoint, Vertex B to the midpoint, and Vertex C to the midpoint)

Next measure the lengths of AD, BD, and CD

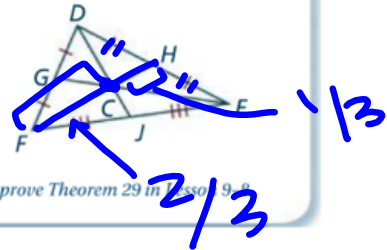
Let's look at some ratios:

take note

Theorem 29 Concurrency of Medians Theorem

The medians of a triangle are concurrent at a point that is two thirds the distance from each vertex to the midpoint of the opposite side.

$$DC = \frac{2}{3}DJ \quad EC = \frac{2}{3}EG \quad FC = \frac{2}{3}FH$$



You will prove Theorem 29 in Lesson 9.9



Problem 1 Finding the Length of a Median

In the diagram at the right, $XA = 8$. What is the length of \overline{XB} ?

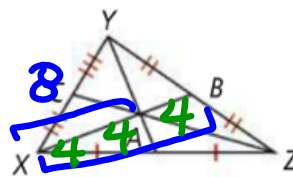
~~$\frac{2}{3}XB = 8$~~

$$\frac{2}{3}XB = 8 \cdot 3$$

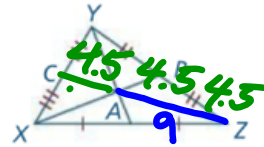
$$\frac{2}{3}XB = 24$$

$$\frac{2}{3}XB = 24$$

$$XB = 12$$

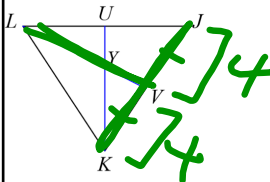


Got It? a. If $ZA = 9$, what is the length of \overline{ZC} ?
 b. Reasoning What is the ratio of ZA to AC ? Explain.



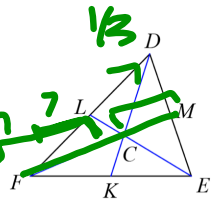
$\overline{ZC} = 13.5$

Find KJ if $VJ = 4$



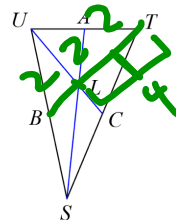
8

Find FM if $CM = 7$



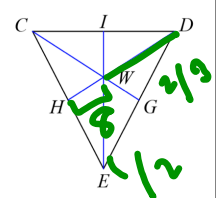
$7 \cdot 3 = 21$

Find TB if $TL = 4$



8

Find DW if $WH = 8$



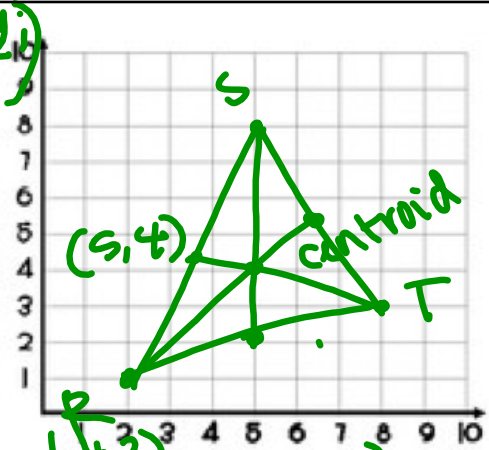
16

› $R(2, 1), S(5, 8), T(8, 3)$ $\left(\frac{x_2+x_1}{2}, \frac{y_2+y_1}{2}\right)$

› Use the midpoint formula to find the midpoint of RT

› Now use the median formula to find the centroid

› Hint: the x value will remain the same

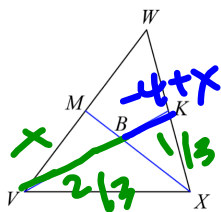


$$\overline{RT} = \left(\frac{2+8}{2}, \frac{1+3}{2}\right) = (5, 2)$$

$$\overline{ST} = \left(\frac{5+8}{2}, \frac{8+3}{2}\right) = (6.5, 5.5)$$

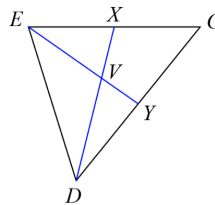
$$\overline{RS} = \left(\frac{2+5}{2}, \frac{1+8}{2}\right) = (3.5, 4.5)$$

1. Find x if $VB = x$ and $BK = -4 + x$



$$x = 2(-4 + x)$$

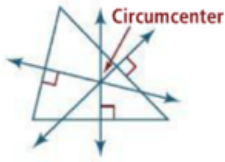
2. Find x if $EV = -6 + 2x$ and $EY = x + 7$



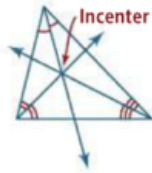
$$-4 + x = -\frac{3x}{2}$$

Take note**Concept Summary Special Segments and Lines in Triangles**

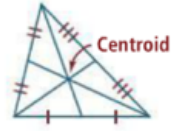
Perpendicular Bisectors



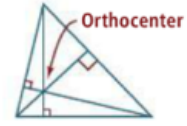
Angle Bisectors



Medians



Altitudes



6.4 Medians and Altitudes of Triangles

Pg 348-350 #s 2, 3-13 odd, 17, 27, 28, 41, 43, 55,
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