

Name: _____ Hour: _____

6.1 A Algebraic Proofs

Give the reason for each statement in the following two-column proof.

1. Given: $3x + 6 = 7x - 2$
Prove: $x = 2$

Statements	Reasons
1. $3x + 6 = 7x - 2$	1. _____
2. $6 = 4x - 2$	2. _____
3. $8 = 4x$	3. _____
4. $2 = x$	4. _____
5. $x = 2$	5. _____

2. Given: $2 - 6x + 4 = 3x - 14 + x$
Prove: $x = 2$

Statements	Reasons
1. $2 - 6x + 4 = 3x - 14 + x$	1. _____
2. $6 - 6x = 3x - 14 + x$	2. _____
3. $6 - 6x = 4x - 14$	3. _____
4. $6 = 10x - 14$	4. _____
5. $20 = 10x$	5. _____
6. $2 = x$	6. _____
7. $x = 2$	7. _____

3. Given: $\frac{1}{4}x + 7y = 10 - y$
 Prove: $x = 40 - 32y$

Statements	Reasons
1. $\frac{1}{4}x + 7y = 10 - y$	1. _____
2. $\frac{1}{4}x + 7y - 7y = 10 - y - 7y$	2. _____
3. $\frac{1}{4}x = 10 - 8y$	3. _____
4. $4\left(\frac{1}{4}x\right) = 4(10 - 8y)$	4. _____
5. $x = 4(10 - 8y)$	5. _____
6. $x = 40 - 32y$	6. _____

4. Given: $\begin{cases} a = 2 \\ -(-2a + 3b) = 6 \end{cases}$
 Prove: $b = -\frac{2}{3}$

Statements	Reasons
1. $-(-2a + 3b) = 6$	1. _____
2. $-2a + 3b = -6$	2. _____
3. $3b = 2a - 6$	3. _____
4. $b = \frac{2}{3}a - 2$	4. _____
5. $a = 2$	5. _____
6. $b = \frac{4}{3} - 2$	6. _____
7. $b = -\frac{2}{3}$	7. _____

5. Given: $5(n-3) = 4(2n-7) - 14$
 Prove: $n = 9$

Statements	Reasons
1. $5(n-3) = 4(2n-7) - 14$	1. _____
2. $5n - 15 = 8n - 28 - 14$	2. _____
3. $5n - 15 = 8n - 42$	3. _____
4. $5n - 15 + 15 = 8n - 42 + 15$	4. _____
5. $5n = 8n - 27$	5. _____
6. $5n - 8n = 8n - 27 - 8n$	6. _____
7. $-3n = -27$	7. _____
8. $\frac{-3n}{-3} = \frac{-27}{-3}$	8. _____
9. $n = 9$	9. _____

6. Given: $4 - 7x = 2x - 23$
 Prove: $x = 3$

Statements	Reasons

7. Given: $\frac{1}{2}x + 6y = 8 - 3y$
Prove: $x = 16 - 18y$

Statements	Reasons

8. Given: $3 - 2x + 12 = 4x - 7 - 2x$
Prove: $\frac{11}{2} = x$

Statements	Reasons

9. Given: $\begin{cases} a = -3 \\ 2b + a + 1 = 5 \end{cases}$
Prove: $b = \frac{7}{2}$

Statements	Reasons

10. Given: $-(n-5) = 2(3n-8) - 7$
Prove: $n = 4$

Statements	Reasons