

Bell Ringer - do #1 and #4

Thursday 12/5

Given a Vertex and a Point on a parabola, write the quadratic function in Vertex Form.

1. Vertex: (1,4) Point: (0,5) 2. Vertex: (-2, 1) Point: (0,2)

$y = a(x-h)^2 + k$
 $5 = a(0-1)^2 + 4$
 $5 = 1a + 4$
 $-4 = -4$

$y = (x-1)^2 + 4$
 $x = 2$
 $-2 - 2$
 $(x-2) = 0$

Given two zeros of a parabola, write a quadratic function in standard form.

~~3. 5, 2~~ 4. $2, -\frac{3}{4}$

$1 = a$

$4x$	$4x^2$	$-8x$
$+3$	$+3x$	-6

$4(x) = \left(-\frac{3}{4}\right) \cdot 4$
 $4x = -3$
 $+3 \quad +3$
 $(4x+3) = 0$

$y = 4x^2 - 5x - 6$

Standards 4A and 4B retakes due Friday 12/20

Must do Review 4A or Review 4B
in order to retake



Goal:

I can use properties of quadratic functions to identify and interpret roots, intercepts and the vertex of a quadratic function in the real world.

Jennifer hit a golf ball and it followed the projectile $h(t) = -16t^2 + 100t$ where t is the time in seconds and h is the height of the ball.

What was the starting height of the ball?

(time, height)
(sec), (ft)



$$t = 0:$$

$$(0, 0)$$

(Note: '0' is labeled 't' and '0' is labeled 'h')


$$\begin{aligned} & -16(0)^2 + 100(0) + 2 \\ & 0 + 0 = 0 \end{aligned}$$

Jennifer hit a golf ball and it followed the projectile $h(t) = -16t^2 + 100t$ where t is the time in seconds and h is the height of the ball.

What was the height of the ball after 2 seconds?

(time, height)

(2, 136)

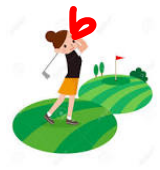
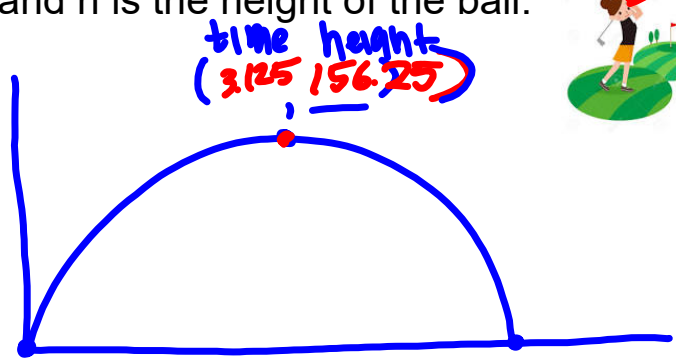

$$h(2) = -16(2)^2 + 100(2) \\ = 136$$

Jennifer hit a golf ball and it followed the projectile $h(t) = -16t^2 + 100t$ where t is the time in seconds and h is the height of the ball.

What was the maximum height the ball reached?

How long did it take to reach the maximum height?

156.25
ft
height
3.125



$(-\frac{b}{2a}, f(\frac{-b}{2a}))$ $h(t) = -16t^2 + 100t$ time

$$\frac{-(-100)}{2(-16)} = \frac{-100}{-32} = \frac{100}{32} = 3.125$$

$-16(3.125)^2 + 100(3.125)$

time height 156.25
 $(3.125, 156.25)$
seconds feet

Jennifer hit a golf ball and it followed the projectile $h(t) = -16t^2 + 100t$ where t is the time in seconds and h is the height of the ball.

For how long was
the ball in the air?

(time, height)

6.25 seconds

$$-16t^2 + 100t = 0$$

$$-4t(4t - 25) = 0$$

$$\begin{array}{r} -4t = 0 \\ \hline -4 \quad -4 \\ t = 0 \end{array}$$

$$\begin{array}{r} 4t - 25 = 0 \\ + 25 \quad + 25 \\ \hline 4t = 25 \\ \hline t = 6.25 \end{array}$$

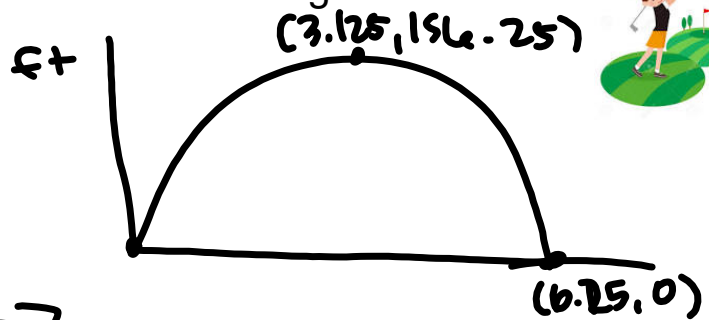


Jennifer hit a golf ball and it followed the projectile $h(t) = -16t^2 + 100t$ where t is the time in seconds and h is the height of the ball.

Give a reasonable domain and range for the scenario.

$$D: [0, 6.25]$$

$$R: [0, 156.25]$$



Jennifer hit a golf ball and it followed the projectile $h(t) = -16t^2 + 100t$ where t is the time in seconds and h is the height of the ball.

How long after she hit the ball was it 80 feet off the ground?

$$-16t^2 + 100t = 80$$

$$-80 \quad -80$$



$$(.94, 80)$$

$$(5.31, 80)$$

$$-16t^2 + 100t - 80 = 0$$

$$-4t^2 + 25t - 20 = 0$$

$$x = \frac{-25 \pm \sqrt{(25)^2 - 4(-4)(-20)}}{2(-4)}$$

$$t = .94$$

$$t = 5.31$$

Given Standard Form

$$f(x) = ax^2 + bx + c$$

How do you find the following?

Starting Height c

Max/Min $Vertex$

Time in air $x\text{-int}$

Domain and Range

$min\text{-}max$ x & y

Height at a specific time

Time at a specific height

$Plug\ in\ time$

$set = height$

due Monday - Standard 4C Tuesday

Applications of Quadratics - Day 1



1. If an M-16 is fired straight upward, then the height $h(t)$ of the bullet in feet at time t in seconds is given by

$$h(t) = -16t^2 + 325t + 4.$$

y-int

a) What is the starting height of the bullet?

(time, height)

$$h(0) = -11$$

$$\cdot 4$$

x-int

b) How long does it take for the bullet to return to the earth?

$$x = \frac{-325 \pm \sqrt{(325)^2 - 4(-16)(4)}}{2(-16)}$$

20.3 seconds

(h,t)

c) What is the maximum height?

$$\left(\frac{-b}{2a}, \right) = \left(\frac{-325}{2(-16)}, \right)$$

(10.16, 1,654.39)

1,654.3 ft

d) What is a realistic domain and range?

time $D: [0, 20.3]$

ft $R: [0, 1,654.39]$

e) At a height of 500 feet how much time has passed?

(1.66, 500)

$$-16t^2 + 325t + 4 = 500$$

$$x = \frac{-325 \pm \sqrt{325^2 - 4(-16)(-496)}}{2(-16)}$$

(18.65, 500)

$$-16t^2 + 325t - 496 = 0$$

2. A contestant tosses a horseshoe from one pit to another with an initial vertical velocity of 50 feet per second. The horseshoe is released 3 feet above the ground. Use the model $h = -16t^2 + 50t + 3$, where h is the height (in feet) and t is the time (in seconds) to tell how long the horseshoe was in the air.

3. The number of mosquitoes $M(x)$, in millions, in a certain area depends on the June rainfall x , in inches, according to the equation $M(x) = 10x - 2x^2$. What rainfall produces the maximum number of mosquitoes?

4. The polynomial function $I(t) = -0.1t^2 + 1.9t$ represents the yearly income (or loss) from a real estate investment, where t is time in years after 1970. During what year does the maximum income occur?

5. Your company uses the quadratic model $y = -7x^2 + 350x$ to represent how many units y of a new product will be sold x weeks after its release. How many units can you expect to sell in week 27?

6. Your company uses the quadratic model $y = -4.5x^2 + 150x$ to represent the average number of new customers who will be signed on x weeks after the release of your new service. How many new customers can you expect to gain in week 8?

7. The profit for a company is given by $P(x) = -0.0002x^2 + 140x - 250000$, where x is the number of units produced. What production level will yield a maximum profit?

8. A boy tosses a ball upward at 32 feet per second from a window that is 48 feet above the ground. The height of the ball above ground (in feet) at time t (in seconds) is given by $h(t) = -16t^2 + 32t + 48$.

a) Find the time at which the ball strikes the ground.

b) At a height of 60 feet how much time has passed?

9. A rock is thrown upward so that its distance, in feet, above the ground after t seconds is $h(t) = -14t^2 + 336t$

a. Find the zeros of the function and explain the meaning in the context of the problem.

b. Find the vertex of the function and explain the meaning in the context of the problem.

c. What is a realistic Domain and Range?

10. John owns a hotdog stand. He has found that his profit is represented by the equation $P(x) = -x^2 + 68x + 77$, with P being the profit in dollars, and x the number of hotdogs sold. How many hotdogs must he sell to earn the most profit?

11. The manufacturer of a CD player has found that the revenue R (in dollars) is $R(p) = -4p^2 + 1280p$, when the unit price is p dollars. If the manufacturer sets the price p to maximize revenue, what is the maximum revenue to the nearest whole dollar?