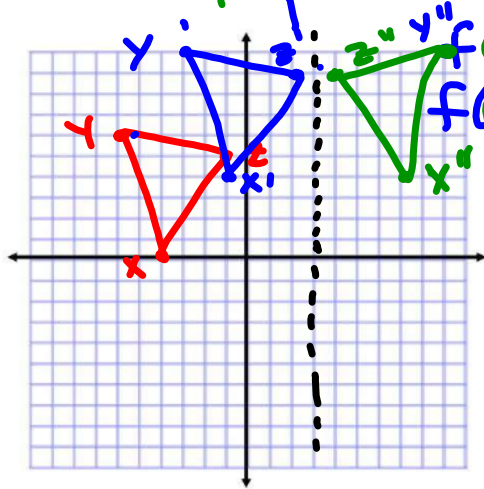


# Bell Ringer

Section 9.4 – Composition of Isometries

1.  $\triangle XYZ$  has vertices  $X(-4, 0)$ ,  $Y(-6, 6)$  and  $Z(-1, 5)$ . What are the coordinates of the vertices of  $(R_x \circ T_{\langle 3, 4 \rangle})(\triangle XYZ)$

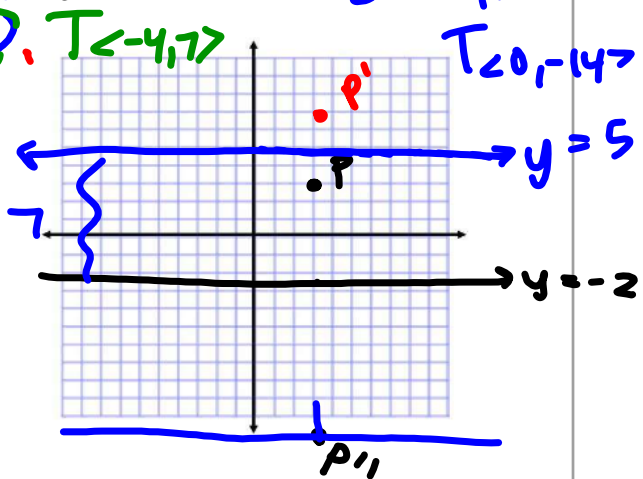
$X''(7, 4)$ ,  $Y''(8, 10)$ ,  $Z''(4, 9)$



2. Write a single transformation rule that has the same effect on the point shown as each composition of transformations.

a.  $T_{\langle -3, 5 \rangle} \circ T_{\langle -1, 2 \rangle}$   
 2nd 1st

b.  $R_{y=-2} \circ R_{y=5}$   
 2nd 1st



3. Write an exponential equation with a y-intercept of 3 and a common ratio of  $\frac{1}{2}$

4. Write a linear equation with a y-intercept of 3 and a slope of  $\frac{1}{2}$

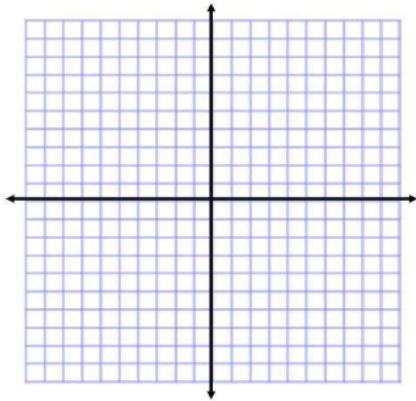
5. Write an exponential equation of a geometric sequence with an initial value of 3 and a common ratio of  $\frac{1}{2}$

## Solutions

### Section 9.4 – Composition of Isometries

1.  $\triangle XYZ$  has vertices  $X(-4, 0)$ ,  $Y(-6, 6)$  and  $Z(-1, 5)$ . What are the coordinates of the vertices of  $(R_{x=3} \circ T_{\langle 3,4 \rangle})(\triangle XYZ)$

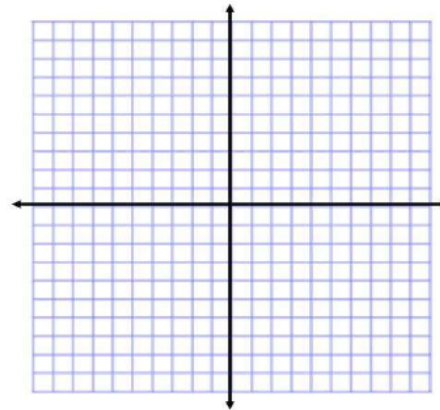
$$X''(7, 4), \quad Y''(9, 10), \quad Z''(4, 9)$$



2. Write a single transformation rule that has the same effect on the point shown as each composition of transformations.

a.  $T_{\langle -3,5 \rangle} \circ T_{\langle -1,2 \rangle}$   
 $T_{\langle -4,7 \rangle}$   
 (left 4 and up 7)

b.  $R_{y=-2} \circ R_{y=5}$   
 $T_{\langle 0,-14 \rangle}$   
 Translates down 14



3. Write an exponential equation with a y-intercept of 3 and a common ratio of  $\frac{1}{2}$

$$y = 3\left(\frac{1}{2}\right)^x$$

4. Write a linear equation with a y-intercept of 3 and a slope of  $\frac{1}{2}$

$$y = \frac{1}{2}x + 3$$

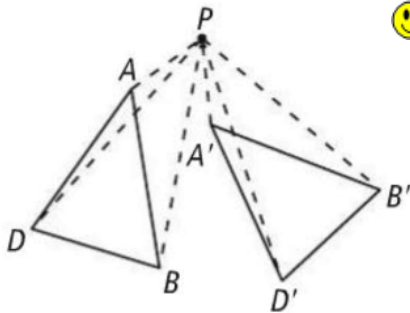
5. Write an exponential equation of a geometric sequence with an initial value of 3 and a common ratio of  $\frac{1}{2}$

$$A(n) = 3\left(\frac{1}{2}\right)^{n-1}$$

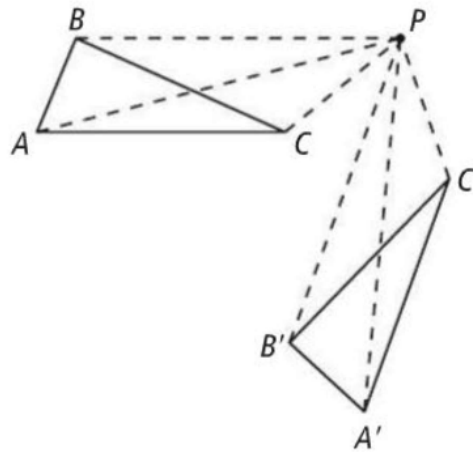
$$a_n = 3\left(\frac{1}{2}\right)^{n-1}$$

correct 9.3 #s 1-4, 7-9, 11-14, 20, 27-32

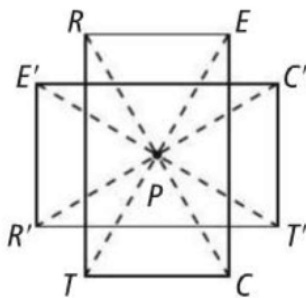
☺ 1.



☺ 7.



2.

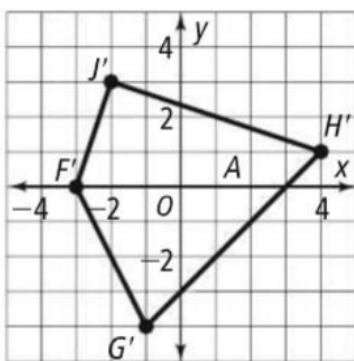


8. R

☺ 9.  $\overline{SE}$

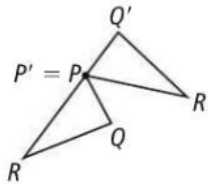
11. Draw  $\overline{AO}$  and  $\overline{A'O}$  and then measure  $\angle AOA'$ .

☺ 3.



☺ 12.

The diagram shows a reflection, not a rotation.  $R'$  is a  $115^\circ$  clockwise rotation of  $R$ . All points of  $\triangle PQR$  must be rotated counterclockwise.

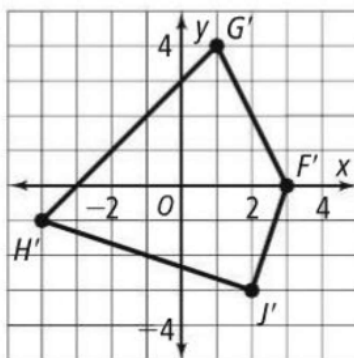


☺ 13.

Both are rigid motions. A reflection reverses orientation. A rotation has the same orientation.

14.  $(-x, -y)$ ; Sample: The coordinates are the same as a single rotation of  $180^\circ$  since  $135^\circ + 45^\circ = 180^\circ$ .

4.



20.  $168.75^\circ$

27. H

28. M

☺ 29.  $\overline{BC}$

30. C

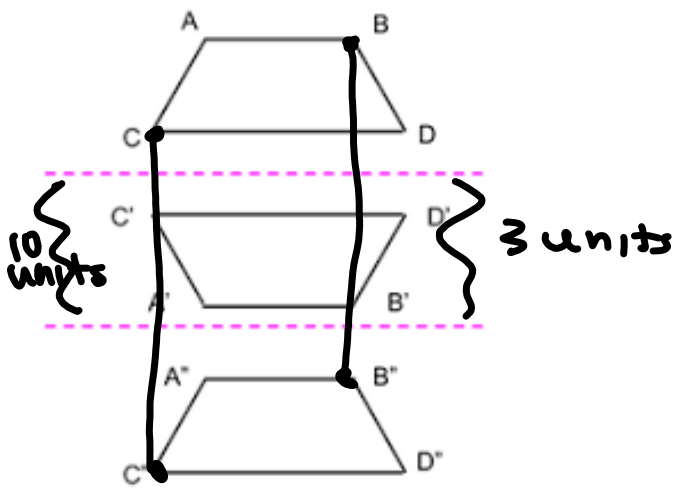
31.  $\overline{LM}$

☺ 32. A

due Wednesday  
9.4 #s 1-8, 10-16 evens, 19-20, 26-32 evens

Hw Tracker due Wednesday

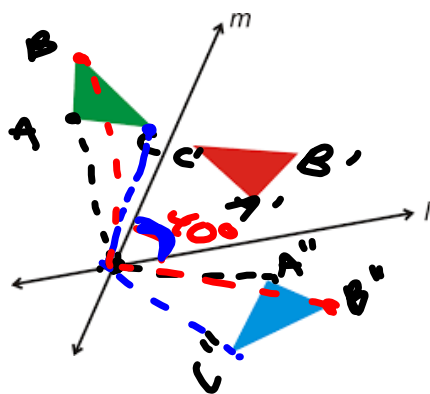
A reflection across 2 parallel lines is the same as one translation



Distance?

double the  
distance  
between || lines

A reflection across two non-parallel lines is the same as one rotation



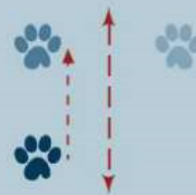
Angle?

double  
angle of  
lines of  
refl.



## Glide Reflection... pg 514

Any composition of isometries can be represented by a reflection, translation, rotation, or glide reflection. A **glide reflection** is the composition of a translation (a glide) and a reflection across a line parallel to the direction of translation. You can map a left paw print onto a right paw print with a glide reflection.



p514



Problem 3

Finding a Glide Reflection Image

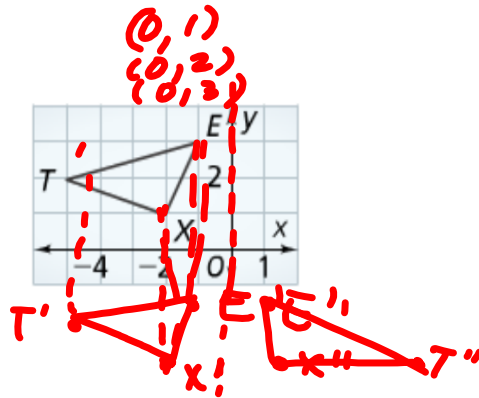
not in book



Coordinate Geometry

What is  $(R_{x=0} \circ T_{\langle 0, -5 \rangle}) (\triangle TEX)$ ?

Which do you do first?



# solution...



**ONLINE PROBLEMS** **Problem 3** Finding a Glide Reflection Image

**Coordinate Geometry** What is  $(R_{x=0} \circ T_{\langle 0, -5 \rangle})(\triangle TEX)$ ?

**Know**

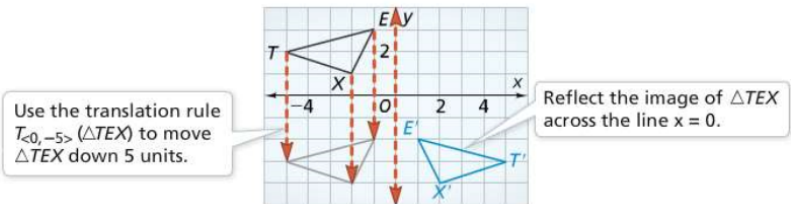
- The vertices of  $\triangle TEX$
- The translation rule
- The line of reflection

**Need**

The image of  $\triangle TEX$  for the glide reflection

**Plan**

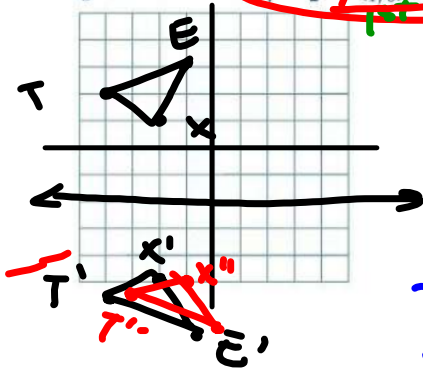
First use the translation rule to translate  $\triangle TEX$ . Then reflect the translation image of each vertex across the line of reflection.



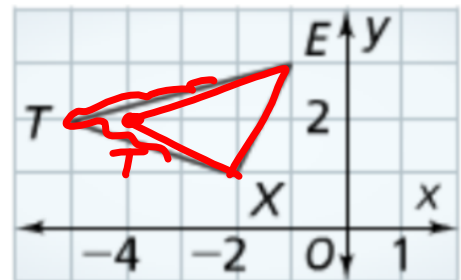
Got it pg 514

$T(-4, 2), E(-1, 3), X(-2, 1)$

**Got It?** Graph  $\triangle TEX$  from Problem 3. What is the image of  $\triangle TEX$  for the glide reflection  $(R_{y=-2}, \langle 1, 0 \rangle)(\triangle TEX)$ ?

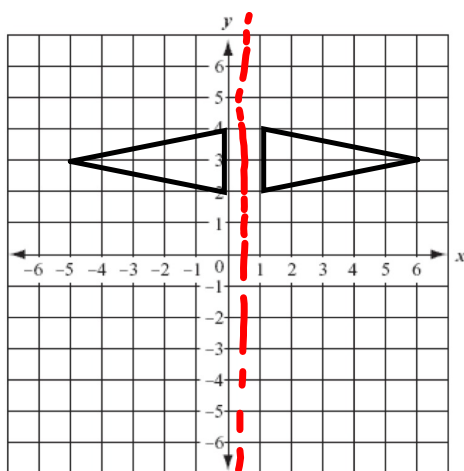


$T'(-3, -6)$   
 $E'(0, -7)$   
 $X'(1, -5)$



p514

State the line of reflection

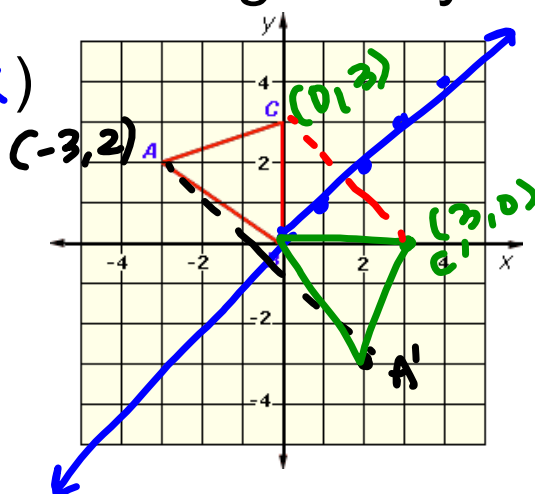


$$x = .5$$

$$x = 0.5$$

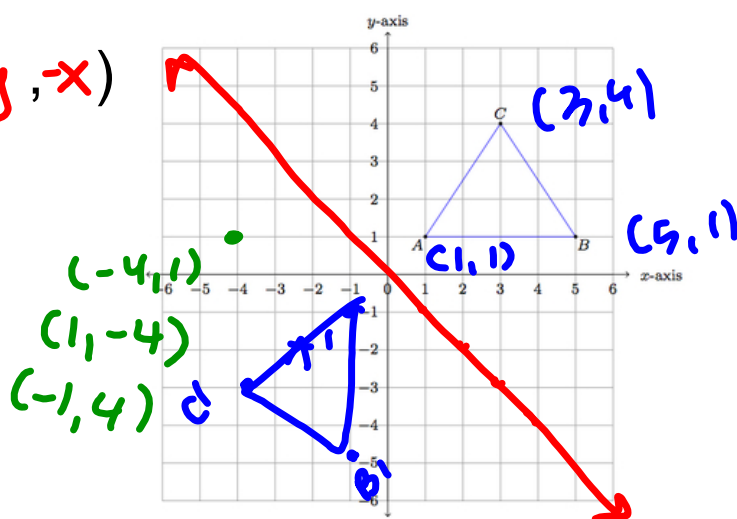
Reflecting over  $y = x$ 

$$(x, y) \rightarrow (y, x)$$



Reflecting over  $y = -x$ 

$$(x, y) \rightarrow (-y, -x)$$



9.4 #s 1-8, 10-16 evens 19-20, 26-32 evens

graph paper for 12,14 &16



Review...

Perform the following Transformation  
 $T_{\langle -4, 2 \rangle}(ABC)$

