

Bell Ringer

Tuesday 12/3

1. Find the common ratio of the geometric sequence

36, 6, 1, $\frac{1}{6}$, ...

0.1, 1, 10, 100, ...

-162, 54, -18, 6, ...

$$r = \frac{1}{6}$$

$$r = 10$$

$$r = -\frac{1}{3}$$

2. Write an equation for the nth term of the geometric sequence. Then find a_{12}

0.6, -3, 15, -75, ...

0.1, 0.9, 8.1, 72.9, ...

$$a_n = 0.6(-5)^{n-1}$$

$$a_n = 0.1(9)^{n-1}$$

$$a_{12} = 0.6(-5)^{11}$$

$$a_{12} = 0.1(9)^{11}$$

$$-29,296,875$$

$$3,138,105,961$$

Week #2 Packet due today - turn in!

Determine if the sequence is arithmetic, geometric or neither.
Justify.

$$1, -16, -33, -50,$$

A $d = -17$

$$-1, -8, -64, -512,$$

G: $r = 8$

$$-39, -13, \left(\frac{13}{3}\right), \left(\frac{13}{9}\right), \dots$$

G: $r = \frac{1}{3}$

$$5, 16, 27, 38,$$

$+11 \quad +11 \quad +11$
A: $d = 11$

Essential Question

How can you define a sequence recursively?

Recursive Equation for an Arithmetic Sequence

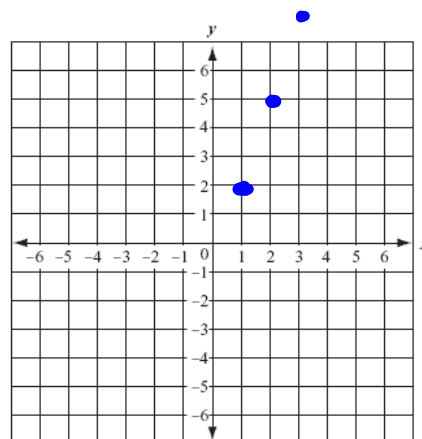
$$a_1 = \underline{\hspace{2cm}}, \quad a_n = a_{n-1} + d$$

25, 20, 15, 10, ...

$$a_1 = 25, \quad a_n = a_{n-1} - 5$$

¹2, ²5, ³8, ⁴11, ...

$$a_1 = 2, \quad a_n = a_{n-1} + 3$$



Recursive Equation for a Geometric Sequence?

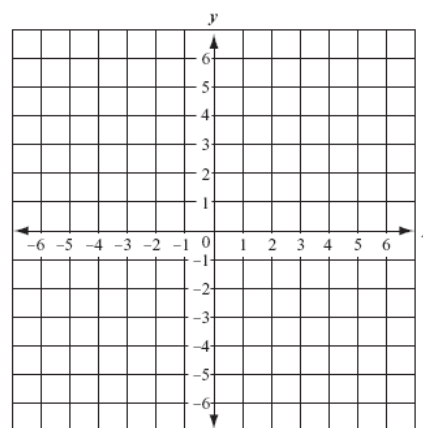
$$a_1 = \underline{\quad}$$

$$2, 4, 8, 16, \dots$$

$$a_1 = 2, a_n = 2a_{n-1}$$

$$1/3, -1, 3, -9, \dots$$

$$a_1 = \frac{1}{3}, a_n = (-3)a_{n-1}$$



Recursive Equation for a Geometric Sequence?

$$a_1 = \underline{\hspace{2cm}}, \quad a_n = r \cdot a_{n-1}$$

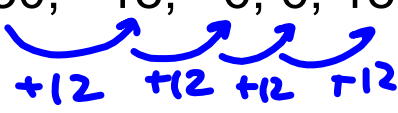
Write the first four terms of each sequence.

a. $\underline{a_1 = 2}, a_n = a_{n-1} + \underline{3}$
 $\underline{2}, \underline{5}, \underline{8}, \underline{11}, \dots$
 a_1, a_2, a_3, a_4

b. $\underline{a_1 = 1}, a_n = \underline{3}a_{n-1}$
 $1, 3, 9, 27, \dots$

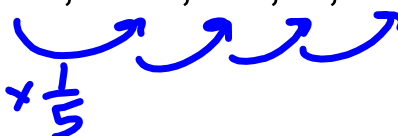
Write a recursive rule for each sequence.

a. $-30, -18, -6, 6, 18, \dots$ $a_1 = -30, a_n = a_{n-1} + 12$



Handwritten notes: $+12$ (under each arrow), $a_1 = -30, a_n = a_{n-1} + 12$ (to the right), and a checkmark with a crossed-out 'b' (further right).

b. $500, 100, 20, 4, 0.8, \dots$ $a_1 = 500, a_n = \frac{1}{5}a_{n-1}$



Handwritten notes: $\times \frac{1}{5}$ (under each arrow), $a_1 = 500, a_n = \frac{1}{5}a_{n-1}$ (to the right), and $a_{n-1}(\frac{1}{5})$ (below the previous equation).

Explicit Rules:

Arithmetic

$$a_n = a_1 + d(n-1)$$
$$a_1 + (n-1)d$$

Geometric

$$a_n = a_1(r)^{n-1}$$

Write an explicit rule for each recursive rule.

a. $a_1 = 25, a_n = a_{n-1} - 10$

$$a_n = 25 - 10(n-1)$$

$$\begin{array}{r} 25 \\ -10n + 10 \\ \hline a_n = 35 - 10n \end{array}$$

, 10

*b. $a_1 = 19.6, a_n = -0.5a_{n-1}$, 19

$$a_n = 19.6(-0.5)^{n-1}$$

Write a recursive rule for each explicit rule.

a. $a_n = -2n + 3$ $a_1 = 1, d = -2$
 $a_1 = 1, a_n = a_{n-1} - 2$

n	a_n
1	1
2	-1
3	-3

$\swarrow -2$
 $\swarrow -2$

b. $a_n = -3(2)^{n-1}$
 $a_1 = -3$

$a_1 = -3, a_n = 2a_{n-1}$

WHITEBOARDS!

Write a recursive rule for the sequence.

1.3, 2.6, 3.9, 5.2, 6.5, . . .

Write a recursive rule for the sequence.

Then write the next three terms of the sequence.

5, 6, 11, 17, 28, . . .

Write an explicit rule for the recursive rule.

$$a_1 = 13, a_n = -3a_{n-1}$$

Write a recursive rule for the explicit rule.

$$a_n = -n + 1$$

Write the first four terms of the sequence.

$$a_1 = 0.7, a_n = 10a_{n-1}$$

Write a recursive rule for the sequence.

4, 20, 100, 500, 2500, . . .

Write a recursive rule for the sequence.

Then write the next three terms of the sequence.

$-3, -4, -7, -11, -18, \dots$

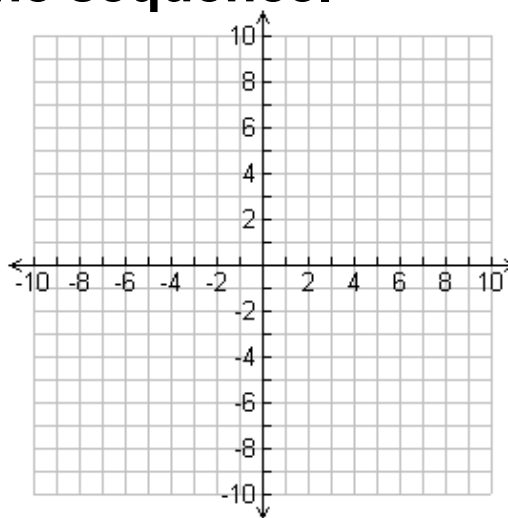
Write a recursive rule for the explicit rule.

$$a_n = -2.5(4)^{n-1}$$

Write the first four terms of the sequence.

Then graph the sequence.

$$a_1 = -10, a_n = \frac{1}{2} a_{n-1}$$



Write the first four terms of the sequence.

$$a_1 = -7.5, a_n = a_{n-1} + 2.5$$

Write a recursive rule for the sequence.

128, -32, 8, -2, 0.5, . . .

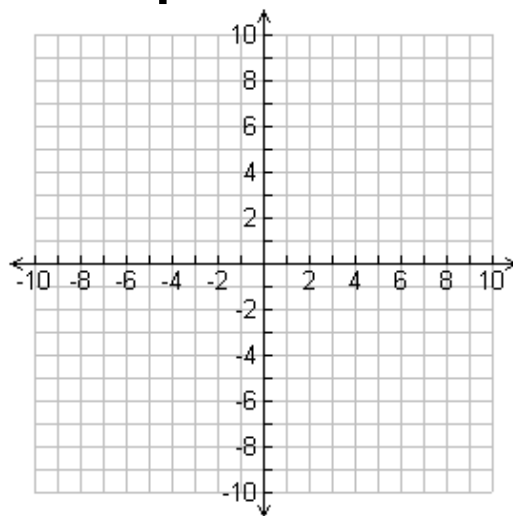
Write an explicit rule for the recursive rule.

$$a_1 = -45, a_n = a_{n-1} + 20$$

Write the first four terms of the sequence.

Then graph the sequence.

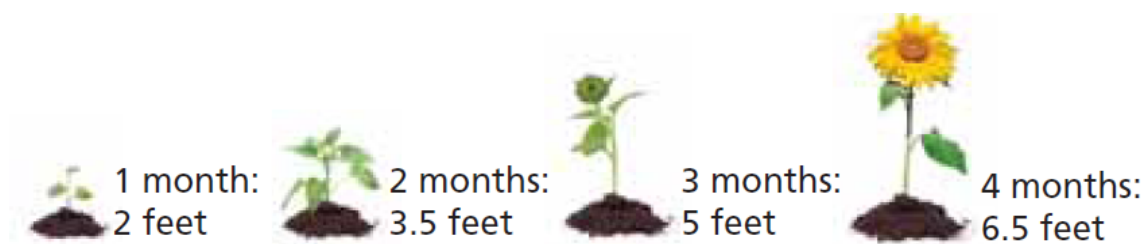
$$a_1 = 0, a_n = a_{n-1} - 2$$



Write a recursive rule for the sequence.

8, 3, -2, -7, -12, . . .

Write a recursive rule for the height of the sunflower over time.



Challenge:

1, $\overset{a_1}{1}$, $\overset{a_2}{2}$, 3, 5, 8, 13, 21, 34

a. Write a recursive rule for the sequence.

$$a_1 = 1 \quad a_n = a_{n-1} + a_{n-2}$$
$$a_2 = 1$$

b. Write the next three terms of the sequence.

13, 21, 34

Challenge:
$$1, 1, 0, -1, -1, 0, 1, 1, \dots$$

- a. Write a recursive rule for the sequence.

- b. Write the next three terms of the sequence.

Challenge:

4, 3, 1, 2, -1, 3, -4, . . .

- a. Write a recursive rule for the sequence.
- b. Write the next three terms of the sequence.

due Thursday
6.6 hw pg 318-320 #s 1, 2, 3-37 odd